## Chemical Equilibrium

Simplifications/assumptions we've been working under:

1. Reactions go to completion (" $\rightarrow$ ")
2. Only the forward reaction is involved
3. Reactions stop when completed

None of these things are strictly true!
What have we learned from kinetics?


## Chemical Equilibrium

Reasonable to write ALL reactions as reversible.

- Requirements?


## Generic Equilibrium:

$$
\begin{gathered}
\stackrel{k_{1}}{\mathrm{aA}+\mathrm{bB}} \rightleftarrows \mathrm{cC}+\mathrm{dD} \\
k_{-1}
\end{gathered}
$$

At equilibrium rate forward = rate reverse

$$
\begin{gathered}
k_{1}\left(\mathcal{A}_{\mathrm{A}}\right)^{\mathrm{a}}\left(\mathcal{A}_{\mathrm{B}}\right)^{\mathrm{b}}=\mathrm{k}_{-1}\left(\mathcal{A}_{\mathrm{C}}\right)^{\mathrm{c}}\left(\mathcal{A}_{\mathrm{D}}\right)^{\mathrm{d}} \\
\mathcal{A}_{\mathrm{A}}=\text { "activity" of compound (or element) } \mathrm{A}
\end{gathered}
$$

## Chemical Equilibrium

Moving all the constants to one side

Activity is a measure of effective reactivity..."opportunity to get involved" in the process of interest.

$$
\mathcal{A}_{\mathrm{A}}=\gamma_{\mathrm{A}}[\mathrm{~A}] \text { (for solutions) or } \mathcal{A}_{\mathrm{A}}=\gamma_{\mathrm{A}} \mathrm{p}_{\mathrm{A}} \text { (for gases) }
$$

In equilibrium considerations, we typically relate (ratio) all conditions to a "reference state", $\mathrm{c}^{\circ}$ (1 M for solutions, 1 atm for gases)

$$
K=\frac{\left(\frac{\gamma_{C}[C]}{c^{0}}\right)^{c}\left(\frac{\gamma_{D}[D]}{c^{0}}\right)^{d}}{\left(\frac{\gamma_{A}[A]}{c^{0}}\right)^{a}\left(\frac{\gamma_{B}[B]}{c^{0}}\right)^{b}}
$$

## Equilibrium Constant Expression

Generic Equilibrium Constant Expressions ("kind of"... $\mathcal{A}$ ):

$$
\mathrm{K}_{\mathrm{c}}=\frac{[C]^{c}[D]^{\mathrm{d}}}{[A]^{a}[B]^{b}}=\frac{\text { products }^{\mathrm{x}}}{[\text { reactants }]^{y}} \quad \mathrm{~K}_{\mathrm{p}}=\frac{\left(\mathrm{p}_{C}\right)^{c}\left(\mathrm{p}_{\mathrm{D}}\right)^{\mathrm{d}}}{\left(\mathrm{p}_{A}\right)^{\mathrm{a}}\left(\mathrm{p}_{\mathrm{B}}\right)^{b}}=\frac{\mathrm{p}_{\text {products }}{ }^{\mathrm{x}}}{\mathrm{p}_{\text {reactants }}{ }^{\mathrm{y}}}
$$

NOTE: K is dimensionless!

## IMPORTANT! CRITICAL! ESSENTIAL! CRUCIAL!

1. In order for a system (reaction) to be at equilibrium, the $\mathrm{K}_{\mathrm{eq}}$ expression MUST be satisfied!!!
2. If the $\mathrm{K}_{\text {eq }}$ expression is satisfied, the system is in equilibrium!

We can use this to predict the extent of a reaction and/or the direction a reaction is likely to proceed.

## Equilibrium Constant Expression

## Expressing $\mathrm{K}_{\mathrm{eq}}$ in various concentrations:

- Gases

Describe $K$ in terms of partial pressures
WHY?

$$
\begin{gathered}
\mathrm{aA}(\mathrm{~g})+\mathrm{bB}(\mathrm{~g}) \rightleftarrows \mathrm{cC}(\mathrm{~g})+\mathrm{dD}(\mathrm{~g}) \\
\mathrm{K}_{\mathrm{p}}=\frac{\left(\mathrm{p}_{\mathrm{C}}\right)^{\mathrm{c}}\left(\mathrm{p}_{\mathrm{D}}\right)^{d}}{\left(\mathrm{p}_{\mathrm{A}}\right)^{2}\left(\mathrm{p}_{\mathrm{B}}\right)^{b}}
\end{gathered}
$$

- Solutions

Describe K in terms of molar concentrations (M)
Often noted at $\mathrm{K}_{\mathrm{c}}$

## Linking Kinetics and Thermodynamics

- Relationship between tendencies and activation parameters
- Thermodynamics and kinetics must cooperate for a reaction to proceed toward products



## Linking Kinetics and Thermodynamics



## Golden Rules of Equilibria

1. $\mathrm{K}_{\mathrm{eq}}$ is dimensionless and constant at a given temperature.
2. When writing equilibrium constant expressions, omit solids, pure liquids, and solvents.

- WHY?

3. Always use smallest integer coefficients when balancing equations and writing $\mathrm{K}_{\text {eq }}$.

$$
\mathrm{H}_{2}+\mathrm{I}_{2} \rightleftarrows 2 \mathrm{HI} \quad 1 / 2 \mathrm{H}_{2}+1 / 2 \mathrm{I}_{2} \rightleftarrows \mathrm{HI}
$$

@ Eq.: $[\mathrm{HI}]=1.58 \mathrm{M},\left[\mathrm{H}_{2}\right]=0.212 \mathrm{M},\left[\mathrm{I}_{2}\right]=0.212 \mathrm{M}$, calculate $\mathrm{K}_{\mathrm{c}}$.

## Golden Rules of Equilibria

4. When a balanced reaction is reversed, $\mathrm{K}_{\text {reverse }}=1 / \mathrm{K}_{\text {forward }}$

$$
\mathrm{H}_{2}+\mathrm{I}_{2} \rightleftarrows 2 \mathrm{HI} \quad \text { vs } \quad 2 \mathrm{HI} \rightleftarrows \mathrm{H}_{2}+\mathrm{I}_{2}
$$

5. When adding reactions, $\mathrm{K}_{\mathrm{eq}}$ for the net reaction is the product of the $\mathrm{K}_{\mathrm{eq}}$ 's for the individual reactions.
Example: Calculate the $\mathrm{K}_{\mathrm{p}}$ for the gas phase reaction:
$\mathrm{H}(\mathrm{g})+\mathrm{Br}(\mathrm{g}) \rightleftarrows \mathrm{HBr}(\mathrm{g})$

| $\mathrm{H}_{2}(\mathrm{~g})+\mathrm{Br}_{2}(\mathrm{~g}) \rightleftarrows 2 \mathrm{HBr}(\mathrm{g})$ | $\mathrm{K}_{1}=7.9 \times 10^{11}$ |
| :---: | :--- |
| $\mathrm{Br}_{2}(\mathrm{~g}) \rightleftarrows 2 \mathrm{Br}(\mathrm{g})$ | $\mathrm{K}_{2}=4.8 \times 10^{-41}$ |
| $\mathrm{H}_{2}(\mathrm{~g}) \rightleftarrows 2 \mathrm{H}(\mathrm{g})$ | $\mathrm{K}_{3}=2.2 \times 10^{-15}$ |

## Golden Rules of Equilibria

6. At equilibrium, the concentrations of reactants and products MUST satisfy the equilibrium constant expression!!

Example: Acetic acid is a weak acid that dissociates via the equilibrium shown below. We dissolve 1.00 mole of acetic acid in 1.00 L of water. After allowing the solution to come to equilibrium, the $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$ is measured to be 0.00423 M . If the equilibrium constant for this process is $1.8 \times 10^{-5}$, what is the ratio of dissociated to undissociated acid?

$$
\mathrm{CH}_{3} \mathrm{COOH}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{I}) \rightleftarrows \mathrm{CH}_{3} \mathrm{COO}^{-}(\mathrm{aq})+\mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})
$$

## Using $\mathrm{K}_{\mathrm{eq}}$ to Predict "Direction" of Reaction

When given a set of conditions (concentrations) ask:

1. Is the system already at equilibrium?
2. If yes, you're done! If no, what does the system need to do to reach equilibrium?

Accomplish (1) by calculating Reaction Quotient (Q): K with nonequilibrium values. Compare Q with $\mathrm{K}_{\mathrm{eq}}$


| $\mathrm{Q}=\mathrm{K}_{\text {eq }}$ | System is in equilibrium |
| :--- | :--- |
| $\mathrm{Q}>\mathrm{K}_{\text {eq }}$ | System too product "heavy" |
| $\mathrm{Q}<\mathrm{K}_{\text {eq }}$ | System too reactant "heavy" |

Accomplish (2) by "mapping" the reaction and doing a little math.

## Using $\mathrm{K}_{\text {eq }}$ to Predict "Direction" of Reaction

Example:

$$
\mathrm{N}_{2}+\mathrm{O}_{2} \rightleftarrows 2 \mathrm{NO}
$$

At 2000K the $\mathrm{K}_{\mathrm{c}}$ for the formation of NO is $4.0 \times 10^{-4}$. You have a container in which, at 2000 K , the concentration of $\mathrm{N}_{2}$ is $0.50 \mathrm{M}, \mathrm{O}_{2}$ is 0.25 M , and NO is $4.2 \times 10^{-3} \mathrm{M}$. Is the system at equilibrium? If not, which direction must the reaction proceed to approach equilibrium? Calculate the equilibrium concentrations of $\mathrm{N}_{2}, \mathrm{O}_{2}$, and NO .


## Le Chatelier's Principle and Bullying Reactions

## Le Chatelier's Principle

Start with system in equilibrium, what happens if we perturb things?

1. Change Concentrations:
2. Change Pressure:
3. Change Temperature:
