

CHEM 130
Quiz 5 – July 21, 2016

Name _____

Complete the following problems. You must show your work to receive full credit. Show your answers to the correct number of significant figures with the correct units.

1. The initial rate for the reaction $A + B \rightarrow C + D$ is determined for different initial conditions, with the results below. Determine the rate law and the value of the rate constant for the reaction. (9 points)

Expt.	[A], M	[B], M	Initial Rate, $M s^{-1}$
1	0.185	0.133	3.35×10^{-4}
2	0.185	0.266	1.35×10^{-3}
3	0.370	0.133	6.75×10^{-4}
4	0.370	0.266	2.70×10^{-3}

From Expt. 1 to Expt. 3, [A] is doubled, while [B] remains fixed. This causes the rate to increase

by a factor of $\frac{6.75 \times 10^{-4} M s^{-1}}{3.35 \times 10^{-4} M s^{-1}} = 2.01 \approx 2$.

Thus, the reaction is first-order with respect to A.

From Expt. 1 to Expt. 2, [B] doubles, while [A] remains fixed. This causes the rate to

increase by a factor of $\frac{1.35 \times 10^{-3} M s^{-1}}{3.35 \times 10^{-4} M s^{-1}} = 4.03 \approx 4$.

Thus, the reaction is second-order with respect to B.

Overall reaction order = order with respect to A + order with respect to B = $1 + 2 = 3$. The reaction is third-order overall.

$$\text{Rate} = 3.35 \times 10^{-4} M s^{-1} = k(0.185 M)(0.133 M)^2$$

$$k = \frac{3.35 \times 10^{-4} M s^{-1}}{(0.185 M)(0.133 M)^2} = 0.102 M^{-2} s^{-1}$$

2. The *half-life* (denoted $t_{1/2}$) is the time it takes for the concentration of a reactant to be decreased to half of its original value. Mathematically, after one half-life $[R] = \frac{1}{2} [R]_0$. Consider the integrated rate law for a first order reaction. If the half-life of the reaction is 949 seconds, what is the rate constant for the reaction (with appropriate units)? (8 points)

The integrated rate law for a first order reaction is $\ln[R]_t = -kt + \ln[R]_0$. From the problem, we are told that at $t=949$ seconds, the $[R]_t = \frac{1}{2} [R]_0$. Inserting these values into the rate law:

$$\ln(0.5[R]_0) = -k(949 s) + \ln[R]_0$$

We do not know $[R]_0$ explicitly, but we can use the rules of logarithms to simplify the expression:

$$\ln(0.5) + \ln[R]_0 = -k(949 s) + \ln[R]_0$$

Subtracting $\ln[R]_0$ from both sides:

$$\ln(0.5) = -k(949 s)$$

Rearranging:

$$k = -(\ln(0.5))/(949 s) = 7.30 \times 10^{-4} s^{-1}$$

3. If even a tiny spark is introduced into a mixture of $\text{H}_2(\text{g})$ and $\text{O}_2(\text{g})$, a highly explosive exothermic reaction occurs. Without the spark, the mixture remains unreacted indefinitely. Explain this observation in terms of the reaction thermodynamics and kinetics. A reaction coordinate diagram may be useful.(8 points)

The activation energy for the reaction of hydrogen with oxygen is quite high, too high, in fact, to be supplied by the energy ordinarily available in a mixture of the two gases at ambient temperatures. However, the spark supplies a suitably concentrated form of energy to overcome the activation barrier and initiate the reaction of at least a few molecules. Since the reaction is highly exothermic, the reaction of these first few molecules supplies sufficient energy for yet other molecules to react and the reaction proceeds to completion or to the elimination of the limiting reactant.

Possibly Useful Information

$R = 0.08206 \text{ L atm mol}^{-1} \text{ K}^{-1}$ $R = 8.314 \text{ J mol}^{-1} \text{ K}^{-1}$	$\ln k = -\left(\frac{E_a}{R}\right)\left(\frac{1}{T}\right) + \ln A$	$k = Ae^{-E_a/RT}$
rate = $k[A]^0$	rate = $k[A]^1$	rate = $k[A]^2$
$[A]_t = -kt + [A]_0$	$\ln[A]_t = -kt + \ln[A]_0$	$\frac{1}{[A]_t} = kt + \frac{1}{[A]_0}$

1 1A	2 2A											13 3A	14 4A	15 5A	16 6A	17 7A	18 8A
¹ H 1.00794																	² He 4.00260
³ Li 6.941	⁴ Be 9.01218											⁵ B 10.811	⁶ C 12.011	⁷ N 14.0067	⁸ O 15.9994	⁹ F 18.9984	¹⁰ Ne 20.1797
¹¹ Na 22.9898	¹² Mg 24.3050	3 3B	4 4B	5 5B	6 6B	7 7B	8 8B	9 8B	10 8B	11 1B	12 2B	¹³ Al 26.9815	¹⁴ Si 28.0855	¹⁵ P 30.9738	¹⁶ S 32.066	¹⁷ Cl 35.4527	¹⁸ Ar 39.948
¹⁹ K 39.0983	²⁰ Ca 40.078	²¹ Sc 44.9559	²² Ti 47.88	²³ V 50.9415	²⁴ Cr 51.9961	²⁵ Mn 54.9381	²⁶ Fe 55.847	²⁷ Co 58.9332	²⁸ Ni 58.693	²⁹ Cu 63.546	³⁰ Zn 65.39	³¹ Ga 69.723	³² Ge 72.61	³³ As 74.9216	³⁴ Se 78.96	³⁵ Br 79.904	³⁶ Kr 83.80
³⁷ Rb 85.4678	³⁸ Sr 87.62	³⁹ Y 88.9059	⁴⁰ Zr 91.224	⁴¹ Nb 92.9064	⁴² Mo 95.94	⁴³ Tc (98)	⁴⁴ Ru 101.07	⁴⁵ Rh 102.906	⁴⁶ Pd 106.42	⁴⁷ Ag 107.868	⁴⁸ Cd 112.411	⁴⁹ In 114.818	⁵⁰ Sn 118.710	⁵¹ Sb 121.757	⁵² Te 127.60	⁵³ I 126.904	⁵⁴ Xe 131.29
⁵⁵ Cs 132.905	⁵⁶ Ba 137.327	⁵⁷ *La 138.906	⁷² Hf 178.49	⁷³ Ta 180.948	⁷⁴ W 183.84	⁷⁵ Re 186.207	⁷⁶ Os 190.23	⁷⁷ Ir 192.22	⁷⁸ Pt 195.08	⁷⁹ Au 196.967	⁸⁰ Hg 200.59	⁸¹ Tl 204.383	⁸² Pb 207.2	⁸³ Bi 208.980	⁸⁴ Po (209)	⁸⁵ At (210)	⁸⁶ Rn (222)
⁸⁷ Fr (223)	⁸⁸ Ra 226.025	⁸⁹ †Ac 227.028	¹⁰⁴ Rf (261)	¹⁰⁵ Db (262)	¹⁰⁶ Sg (266)	¹⁰⁷ Bh (264)	¹⁰⁸ Hs (277)	¹⁰⁹ Mt (268)	¹¹⁰ Ds (271)	¹¹¹ Rg (272)							

*Lanthanide series	⁵⁸ Ce 140.115	⁵⁹ Pr 140.908	⁶⁰ Nd 144.24	⁶¹ Pm (145)	⁶² Sm 150.36	⁶³ Eu 151.965	⁶⁴ Gd 157.25	⁶⁵ Tb 158.925	⁶⁶ Dy 162.50	⁶⁷ Ho 164.930	⁶⁸ Er 167.26	⁶⁹ Tm 168.934	⁷⁰ Yb 173.04	⁷¹ Lu 174.967
†Actinide series	⁹⁰ Th 232.038	⁹¹ Pa 231.036	⁹² U 238.029	⁹³ Np 237.048	⁹⁴ Pu (244)	⁹⁵ Am (243)	⁹⁶ Cm (247)	⁹⁷ Bk (247)	⁹⁸ Cf (251)	⁹⁹ Es (252)	¹⁰⁰ Fm (257)	¹⁰¹ Md (258)	¹⁰² No (259)	¹⁰³ Lr (262)